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Explore the Midpoint Quadrilateral of a Kite

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Prerequisites and Objectives

- Students already know the kite and its sketchometry construction.
- Students construct the midpoints of the sides of the kite and investigate the new quadrilateral.
- ► Students explain why this quadrilateral is a rectangle.

sketchometry Instructions

Students should know

- how to reflect a point through a line,
- how to construct the midpoint of a line segment,
- how to tag angles,



Measure > tap line segment > tap the screen at a free spot to place the measurement

Further Exploration and Tasks

- Do you know other quadrilaterals (besides kites) where the diagonals are perpendicular to one another?
- Construct the midpoint quadrilateral of these quadrilaterals.
- Prove: Are the diagonals of a quadrilateral perpendicular to one another then the corresponding midpoint quadrilateral is a rectangle.





Explore the Midpoint Quadrilateral of a Kite

Construction

- Construct the kite ADBC.
- Construct the midpoints of the sides of the kite ADBC.
- Connect these midpoints to obtain another quadrilateral EFGH (midpoint quadrilateral).



Exploration

- Drag any of the vertices A, B, C, and D of the kite and observe the midpoint quadrilateral EFGH. Describe its shape.
- Write down your conjecture in your study journal and try to give a proof.
- Does only the kite have this midpoint property?
 Investigate other types of quadrilaterals and make conjectures.
- ► Try to explain (prove) your conjectures in your study journal.



Explore the Midpoint Quadrilateral of a Kite

Which shape does the midpoint quadrilateral of a kite have?
 Write down your conjecture.

 Draw the second diagonal of the kite ADBC. Consider the triangles CDB and DCA. Then the triangles ABC and BAD. Now try to prove your conjecture.

Look for other shapes of quadrilaterals that have the same kind of a midpoint quadrilateral as the kite.