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## Explore the Midpoint Quadrilateral of a Kite

## Prerequisites and Objectives

- Students already know the kite and its sketchometry construction.
- Students construct the midpoints of the sides of the kite and investigate the new quadrilateral.
- Students explain why this quadrilateral is a rectangle.


## sketchometry Instructions

## Students should know

- how to reflect a point through a line,

- how to construct the midpoint of a line segment,

- how to tag angles,
- how to measure line segments.



## Further Exploration and Tasks

- Do you know other quadrilaterals (besides kites) where the diagonals are perpendicular to one another?
- Construct the midpoint quadrilateral of these quadrilaterals.
- Prove: Are the diagonals of a quadrilateral perpendicular to one another then the corresponding midpoint quadrilateral is a rectangle.

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## Explore the Midpoint Quadrilateral of a Kite

## Construction

- Construct the kite ADBC.
- Construct the midpoints of the sides of the kite ADBC.
- Connect these midpoints to obtain another quadrilateral EFGH (midpoint quadrilateral).



## Exploration

- Drag any of the vertices $A, B, C$, and $D$ of the kite and observe the midpoint quadrilateral EFGH. Describe its shape.
- Write down your conjecture in your study journal and try to give a proof.
- Does only the kite have this midpoint property? Investigate other types of quadrilaterals and make conjectures.
- Try to explain (prove) your conjectures in your study journal.


## Explore the Midpoint Quadrilateral of a Kite

- Which shape does the midpoint quadrilateral of a kite have?

Write down your conjecture.

- Draw the second diagonal of the kite ADBC. Consider the triangles CDB and DCA. Then the triangles ABC and BAD. Now try to prove your conjecture.
- Look for other shapes of quadrilaterals that have the same kind of a midpoint quadrilateral as the kite.

